

$$f(x) = bx + c \quad \mathbb{R}$$

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$$(X, f), \quad f : X \rightarrow X \text{ e}$$

$$x = x_0 = f^0(x), x_1 = f(x_0), x_2 = f(x_1), \dots, x_{n+1} = f(x_n) = f^{n+1}(x),$$

$$x_0, x_1, \dots, x_{n+1}, \dots$$

f

$$f^n(x) = f(f(\dots(f(x))\dots))$$

f

$$\text{orb}(x) = \{Z \mid z = f^n(x), n \in \mathbb{N}_0\}.$$

( )

$$f(x) = x \text{ (orb}(x) = \{x\}).$$

f

n > 1

$$f^n(x) = x \quad f^{n-1}(x) \neq x.$$

n

orb(x)

n

orb(x)

$$f(x), f^2(x), \dots, f^n(x)$$

( )

$$x_{n+1} = f(x_n)$$

(X, f) (

$$f : X \rightarrow X \text{ e } )$$

$$\mathbb{R}, \quad f(x) = bx + c$$

$$x_{n+1} = f(x_n) = bx_n + c.$$

$$\mathbb{R}, \quad f(x) = bx + c$$

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$$f(x) = bx + c$$

$$: \quad \mathbb{R} \times \mathbb{R}$$

$$f(x) \quad y=x.$$

$$f^2(x).$$

$$f(x).$$

$$f(x).$$

$$f(x)$$

= .

$$f(x),$$

$$f^2(x).$$

$$( \quad f^k(x) \quad k-$$

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$$f(x)).$$

orb(x).

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$$y = f(x) ($$

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:

1.  $|f'(x)| > 1$  ;
2.  $|f'(x)| < 1$  .

$$f(x) = bx + c \quad R.$$

$$f(x) = bx + c \quad ,$$

$$f(x) = x \Rightarrow bx + c = x \Rightarrow x = \frac{c}{1-b}, b \neq 1.$$

$$f(x) = bx + c \quad f'(x) = b,$$

$$f(x) = bx + c \quad R$$

$$x = \frac{c}{1-b}, b \neq 1$$

b. :

1.  $b \neq 0 \quad c = 0, \quad f(x) = bx$

$$|f'(x)| = |b|.$$

1.  $b > 0 \quad b \neq 1$

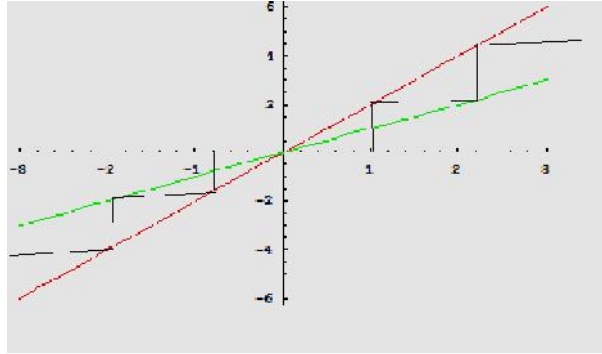
$$x = \frac{c}{1-b} = \frac{0}{1-b} = 0.$$

- i)  $b > 1, f(x) = bx \quad |f'(x)| = |b| > 1, \quad x = 0$

$$f(x) = bx.$$

- 1:  $f(x) = 2x \quad |f'(x)| = 2 > 1, \quad x = 0$

$$f(x) = 2x \quad (1).$$



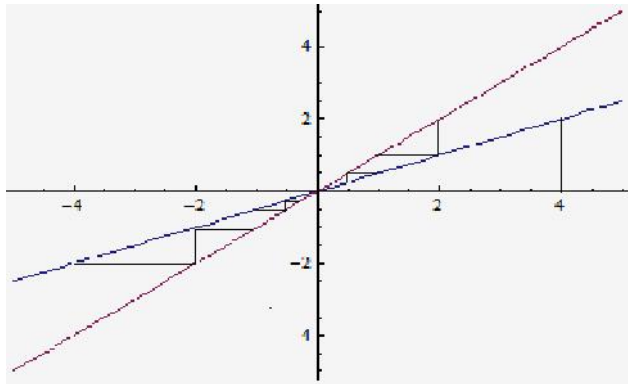
1:  $f(x) = 2x \quad orb(1), orb(-0.8)$

- ii)  $0 < b < 1, f(x) = bx \quad |f'(x)| = |b| < 1, \quad x = 0$

$$f(x) = bx.$$

- 2:  $f(x) = \frac{x}{2} \quad |f'(x)| = \frac{1}{2} < 1, \quad x = 0$

$$f(x) = \frac{1}{2}x \quad (2).$$



2:  $f(x)=x/2$  orb(4), orb(-4)

2.  $b < 0$ ,

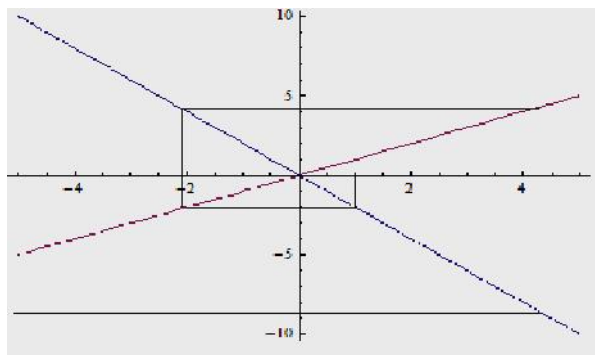
$$x = \frac{c}{1-b} = \frac{0}{1-b} = 0.$$

i)  $b < -1$ ,  $f(x) = bx$   $|f'(x)| = |b| > 1$ ,  $x=0$

$$f(x) = bx.$$

3:  $f(x) = -2x$   $|f'(x)| = 2 > 1$ ,  $x=0$

$$f(x) = -2x \quad (3).$$



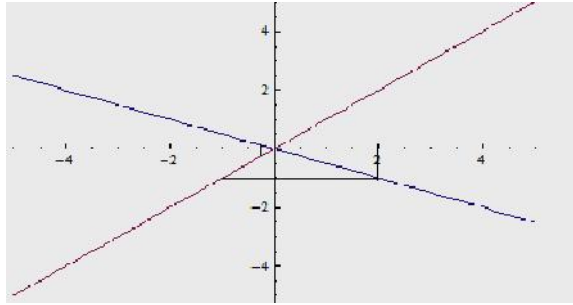
3:  $f(x) = -2x$  orb(1)

ii)  $-1 < b < 0$ ,  $f(x) = bx$   $|f'(x)| = |b| < 1$ ,  $x=0$

$$f(x) = bx.$$

4:  $f(x) = -\frac{1}{2}x$ ,  $|f'(x)| = \frac{1}{2} < 1$ ,  $x=0$

$$f(x) = -\frac{1}{2}x \quad (4).$$



4:  $f(x) = -x/2$  orb(2)

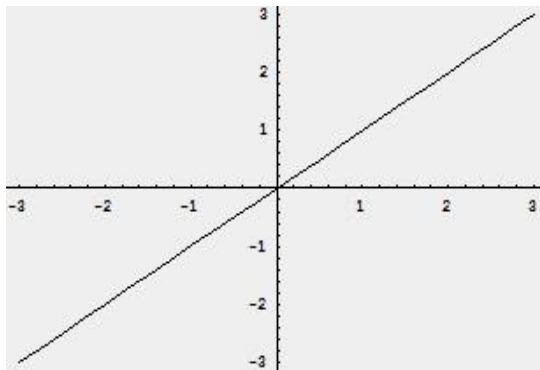
iii)  $b = -1, f(x) = -x \quad |f'(x)| = 1.$

$f(x) = -x, f^2(x) = f(f(x)) = x$

$f(x) = x.$

$f(x) = -x, \quad 0$

3.  $b=1 \quad 2. \quad f(x) = x, \quad |f'(x)| = 1.$   
( 5).



5:  $f(x) = x$

2.  $b=0 \quad c=0 \quad f(x) = 0 \quad . \quad - \quad .$

$f(x) = 0 \quad 0 \quad .$

3.  $b=0, c \neq 0 \quad f(x) = c \quad f'(x) = 0.$

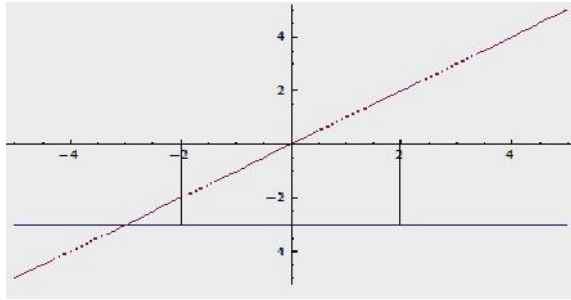
$x = \frac{c}{1-b} = \frac{c}{1} = c.$

$f(x) = c$

$f(x) = c.$

5:  $f(x) = -3 \quad = -3.$

$f(x) = -3 \quad = -3 \quad ( \quad 6).$



6:  $f(x) = -3$

4.  $b \neq 0$   $c \neq 0$   $f(x) = bx + c$   $|f'(x)| = |b|$ .

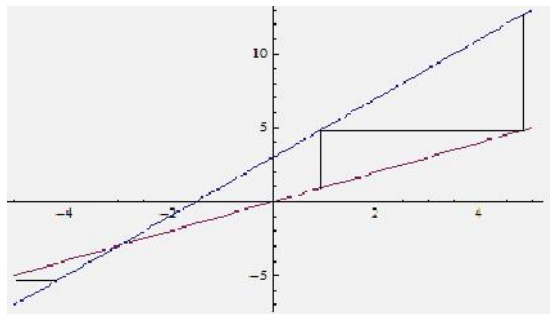
$$x = \frac{c}{1-b} = -\frac{c}{b-1} \quad b \neq 1.$$

i)  $b > 1$   $b < -1$ ,  $f(x) = bx + c$   $|f'(x)| = |b| > 1$ ,

$$x = -\frac{c}{b-1} \quad f(x) = bx + c.$$

6:  $f(x) = 2x + 3$   $|f'(x)| = 2 > 1$ ,

$$x = -\frac{c}{b-1} = -\frac{3}{2-1} = -3 \quad f(x) = 2x + 3 \quad (7).$$



7:  $f(x) = 2x + 3$   $orb(-1)$ ,  $orb(-3.5)$

ii)  $0 < b < 1$   $-1 < b < 0$ ,  $f(x) = bx + c$   $|f'(x)| = |b| < 1$ ,

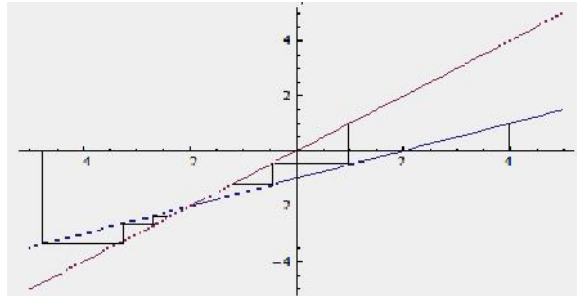
$$x = -\frac{c}{b-1}$$

$$f(x) = bx + c.$$

7:  $f(x) = \frac{1}{2}x - 1$   $|f'(x)| = \frac{1}{2} < 1$ ,

$$x = -\frac{c}{b-1} = -\frac{-1}{\frac{1}{2}-1} = -\frac{-1}{-\frac{1}{2}} = -2 \quad f(x) = \frac{1}{2}x - 1$$

( 8).



8:  $f(x) = x/2 - 1$  orb(4), orb(-4.5)

iii)  $b=-1, c \neq 0, f(x) = -x + c \quad |f'(x)| = |-1| = 1,$

$$x = -\frac{c}{-1-1} = \frac{c}{2}$$

$$f^2(x) = f(f(x)) = f(-x+c) = -(-x+c) + c = x.$$

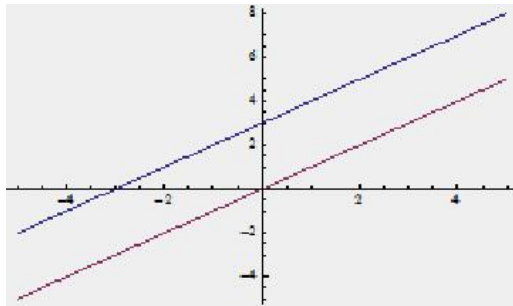
$$f(x) = -x,$$

$$f(x) = -x + c,$$

5.  $b=1, c \neq 0, f(x) = x + c \quad |f'(x)| = |b| = 1$

$$f(x) = x. \quad f(x) = x + c =$$

10:  $f(x) = x + 3 \quad |f'(x)| = 1,$   
( 9).



9:  $f(x) = x + 3$

$f(x) = -x$  ,  $f(x) = bx + c$   $R$   
 2.  $R$

Статијата прв пат е објавена во списанието СИГМА на Сојузот на математичарите на Македонија